Quantitative Macro-Labor: Expectations and Belief Formation

Professor Griffy

Fall 2024

Announcements

- ▶ Briefly review beliefs and rational expectations.

- ▶ Show a model of inequality derived from beliefs.

- ▶ Presentation schedule?

Schedule

► Thursday (11/21)? 1 end of class

► Tuesday (12/3)? 3 people (25 mins each)

► Thursday (12/5)? 3 people (25 mins each)

Portfolio Problem

▶ Consider a portfolio allocation problem in which an agent chooses between one of two assets:

    1. Asset a_{safe} offers a return of r_F, which is known with certainty.

    2. Asset a_{risky} offers a return of r_R, $r_R > r_F$ with probability λ and 0 with probability $(1 - \lambda)$,

▶ Agents maximize a static portfolio problem:

$$V(m) = \max_{a_{safe}, a_{risky}} \lambda u(c'_H) + (1 - \lambda)u(c'_L) \qquad (1)$$

$$c'_H = (1 + r_F)a_{safe} + (1 + r_R)a_{risky} \qquad (2)$$

$$c'_L = (1 + r_F)a_{safe} + a_{risky} \qquad (3)$$

$$m = a_{safe} + a_{risky} \qquad (4)$$

Parameter Uncertainty

▶ What if λ is type-specific?

▶ Asset a_{risky} offers a return of r_R

  1. with probability λ_H for a high-type and λ_L for a low-type

  2. and 0, with probability $(1 - \lambda_H)$ for a high-type and $(1 - \lambda_L)$ for a low-type.

  3. Agents endowed with prior belief that they are high type, $\theta^i \in [0, 1]$

▶ Prior beliefs drawn from uniform distribution $g(\theta^i) \sim U(0, 1)$.

▶ Belief distribution is agent-specific: $h(\theta^i)$ may differ based on history. Initially $h(\theta^i) = g(\theta^i) = \theta$

▶ For simplicity ignore bandit problem.

Signal Extraction

- Bayes theorem:

$$h(\theta'|c') = \frac{f(c'|\lambda)b(\lambda|\theta)g(\theta)}{f(y)} \tag{5}$$

- Binomial likelihood:

$$f(c_H|\lambda) = \lambda^{1_{c'=c_H}}(1-\lambda)^{1-1_{c'=c_H}} \tag{6}$$

- Binomial likelihood:

$$b(\lambda|\theta) = \lambda_H \text{with prob.} \theta = \lambda_L \text{with prob.}(1-\theta) \tag{7}$$

- Prior Distribution ($U(0,1)$):

$$g(\theta) = \theta, \theta \in [0,1], \ 0 \ \textit{else} \tag{8}$$

- Updating ($f(y) = 1$):

$$h(\theta'|c' = c_H') = \frac{\lambda_H \theta}{\lambda_H \theta + \lambda_L(1-\theta)} \tag{9}$$

$$h(\theta'|c' = c_L') = \frac{(1-\lambda_H)\theta}{(1-\lambda_H)\theta + (1-\lambda_L)(1-\theta)} \tag{10}$$

Discussion

- Updating ($f(y) = 1$):

$$h(\theta'|c' = c_H') = \frac{\lambda_H \theta}{\lambda_H \theta + \lambda_L(1 - \theta)} \tag{11}$$

$$h(\theta'|c' = c_L') = \frac{(1 - \lambda_H)\theta}{(1 - \lambda_H)\theta + (1 - \lambda_L)(1 - \theta)} \tag{12}$$

- Thoughts about this updating:

  - What could be subjective here?

  - What could be general equilibrium here?

Beliefs and Affirmative Action in Employment

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[2]University of Virginia

Summer 2023

Motivation

- ▶ Large and persistent earnings gaps between Black and White.

- ▶ 58% explained by occupational choice (CPS).

- ▶ Black teens who believe they will be discriminated against

    - ▶ aspire to lower-pay, less-prestigious occupations,

    - ▶ with more Black representation (this paper).

- ▶ Changing representation change beliefs & raise human capital?

- ▶ Can Affirmative Action permanently reduce racial inequality?

What We Do

- ▶ Develop a model with two-sided beliefs and learning:

    - ▶ workers have beliefs about discrimination in the labor market;

    - ▶ firms have beliefs & preferences over worker productivity by race;

    - ▶ both sides update beliefs after observing labor market outcomes.

- ▶ Use model to assess impact of Affirmative Action on

    - ▶ Black human capital investment and employment beliefs;

    - ▶ firm beliefs about Black human capital.

- ▶ Compare short-run costs and long-run benefits of policy.

Preview of Findings

- In the absence of Affirmative Action:

    - Historical underrepresentation leads Black workers to anticipate discrimination.

    - This causes underinvestment in human capital.

    - The average Black candidate is less qualified, causing firms to statistically discriminate.

    - Causes more pessimism among new Black workers and repeats.

    - Slow convergence to steady-state.

- Black income 75% of White income ($\approx$ same as data)

Preview of Findings

- ▶ After Affirmative Action implemented:

    - ▶ Increase in employment causes optimistic beliefs among next generation of Black workers.

    - ▶ Recognition that most discrimination is statistical & and can be overcome by investment.

    - ▶ Causes an increase in human capital investment, and reverses cycle.

    - ▶ Rapid convergence.

- ▶ Black income 89% of White income *after Affirmative Action*.

- ▶ Although there are short-term costs (underqualified, reinforce stereotypes, etc.), they are outweighed by long-term gains.

Evidence about Beliefs and Occupational Choice

- ▶ Do beliefs about discrimination change occupational choice?

- ▶ NLSY79 contains Qs about

    - ▶ Aspired occupation (ages 12-16);

    - ▶ Occupational prestige index;

    - ▶ Belief that discrimination will affect career.

- ▶ Empirical Specification:

$$ln(Income_i) = \beta_0 + \beta_1 \times 1_i^{Black} + \beta_2 \times 1_i^{Belief} + \beta_3 \times 1_i^{Black} \times 1_i^{Belief}$$
$$+ \beta_4 AFQT_i + \delta X_i + \epsilon_i$$

- ▶ $\beta_1 + \beta_3 < 0$: Beliefs about discrimination negatively affect career aspirations.

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	Prestige Score of Career Aspiration in 1979	Aspired Occupational Income, 1970s
Black ×	-0.2008***	-0.4766**
Believes Discrim. will Affect Career	(0.0159)	(0.1213)
Test: $H_0 : \beta_1 + \beta_3 = 0$	-0.053***	-0.341***
SE	0.0159	0.0730
Observations	1296	1164

Clustered standard errors in parentheses

* p< 0.1, ** p< 0.05, *** p< 0.01

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▶ Robustness (realized occupations, levels, racial composition of occupations): ▶ link

Model Overview

- ▶ During current period
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    - ▶ firms receive set of applications & hire "best" applicant.

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  - ▶ New cohort of workers born, update beliefs about discrimination ($\hat{\eta}$) based on aggregate hiring;
  - ▶ firms update beliefs about productivity by race ($f(z|r)$) based on workers interviewed & hired.

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- ▶ Discrimination:

  - ▶ Some firms are perm. taste-based discriminators (measure μ), but identities unknown.
  - ▶ all firms statistically discriminate based on history ($f(z|r)$),
  - ▶ workers believe measure $\hat{\eta}$ are taste-based discrim., but can't distinguish sources.

Worker Static Optimization

- Workers initial state:

  - Race, r, innate ability $q \sim LN(\mu_Q, \sigma_Q)$

  - Employment beliefs $\hat{P}(e|z, r; \hat{\eta})$

- Workers problem:

  - Make costly human capital investment decision, z, $(\frac{\partial c(z)}{\partial q} < 0)$.

  - Apply to high prestige job with cost $\nu \sim$ *Gumbel*,

  - believe prob $\hat{P}$ of job offer.

Firm Static Optimization

▶ Firm state: Beliefs $f_i(z|r) \sim Beta(\alpha, \beta)$ with prior $p(\alpha, \beta)$.

▶ Firm's problem: Receive $H \sim exp(\lambda)$ applications,

  ▶ get noisy signal $y_j = ln(z_j) + \epsilon_j$, $\epsilon \sim N(0, \sigma_\epsilon)$

  ▶ assign score $s_i(y, r, T, f) = E[z|y, r, f] - 1_D^B \gamma + 1_{AA}^B \xi$

  ▶ And hire $\max\{s_1, ..., s_{H_i}\}$.

▶ Labor market resolution:

  ▶ of N firms, e^B hire Black workers and e^W hire White.

Workers updating beliefs I

▶ What they know:

  ▶ Aggregate hiring outcomes by race, e_j^B, $e_j^W \forall j \leq t$,

  ▶ Prev. hire preds. $\hat{e}_j^r(\hat{\eta}) = \int_q \hat{P}_j(e|z, r; \hat{\eta}) \frac{\partial z_j(q, r)}{\partial q} dF(q) \forall j < t$

  ▶ Current period decision rules & q dist. params.

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    - ▶ Current period decision rules & q dist. params.

- ▶ Need $\hat{P}_t(e|z, r; \hat{\eta})$. Approximate firm problem:

    - ▶ Calc. scores w/ unbiased beliefs: $s(y, r, T) = y - 1_D^B \gamma + 1_{AA}^B \xi$

    - ▶ Use to calc. $\hat{P}(.; T) = P(s_j = \max\{s_1, ..., s_H\}|z, r, T)$ (signal)

    - ▶ Use $z_t(q, r)$ and μ_q, σ_q to est. $e_t^r(T)$.

- ▶ Yields $e_t^r(D)$ and $e_t^r(N)$,

- ▶ Compare to realized employment to update $\hat{\eta}$ and $\hat{P}$.

Workers updating beliefs II

- Next cohort knows history of:

  - hiring by race $\{(e_0^B, e_0^w), ..., (e_{t-1}^B, e_{t-1}^w)\}$

  - predicted outcomes: $\{\hat{e}_0^r(e|r; \hat{\eta}), ..., \hat{e}_{t-1}^r(e|r; \hat{\eta})\}$

  - where $\hat{e}^r(e|B; \hat{\eta}) = \hat{\eta}\hat{e}^r(e|B, D) + (1 - \hat{\eta})\hat{e}^r(e|B, N)$

- Updates $\hat{\eta}$ to minimize difference between this history:

$$\min_{\hat{\eta}} \sum_{j=0}^{t-1} \left(\frac{\hat{e}_j^r(e|B; \hat{\eta})}{\hat{e}_j^r(e|B; \hat{\eta}) + \hat{e}_j^r(e|W; \hat{\eta})} - \frac{e_j^B}{e_j^B + e_j^W} \right)^2 \qquad (13)$$

Workers updating beliefs II

- ▶ Next cohort knows history of:

    - ▶ hiring by race $\{(e_0^B, e_0^w), ..., (e_{t-1}^B, e_{t-1}^w)\}$

    - ▶ predicted outcomes: $\{\hat{e}_0^r(e|r; \hat{\eta}), ..., \hat{e}_{t-1}^r(e|r; \hat{\eta})\}$

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- ▶ Use new $\hat{\eta}$ to find $\hat{P}(e|z, r; Z^0, \hat{\eta})$,

- ▶ then iterate to find $(Z^0, \hat{P})$ fixed point for next cohort beliefs.

Firms updating beliefs I

- ▶ Firm only cares about maximizing z given preferences.

- ▶ Firm information carried over from previous period:

  - ▶ Learned true productivity z of hired worker (and their race).

  - ▶ knows (y, r) of all interviewees.

  - ▶ sample of own hires/interviewees $X = \{\{\rightharpoonup y, \rightharpoonup r\}, (y, z, r)\}$.

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- ▶ Firm has belief about distribution of z, $f(z|r)$, by race:

  - ▶ prior over distributional parameters of $f(z|r) \sim Beta(\alpha, \beta)$.

  - ▶ Bayesian update weight on different α & β values based on new sample, X.

Firms updating beliefs II

- ▶ Each firm has prior and new information:

  - ▶ prior, $p(\alpha, \beta)$ (over $f(z|r) \sim Beta(\alpha, \beta)$).
  - ▶ sample of own hires/interviewees $X = \{\{\rightharpoonup y, \rightharpoonup r\}, (y, z, r)\}$.

- ▶ they calc. $p(X|\alpha, \beta)$ for parameter space of (α, β) & update:

$$p(X|\alpha, \beta) = \Pi_{i=1}^{H} \underbrace{\left(\int \frac{e^{-\frac{1}{2}\left(\frac{y_i - ln(z)}{\sigma}\right)^2}}{2\sqrt{\pi}\sigma} f(z|r) dz \right)^{1 - 1_{s_i = \hat{s}}}}_{\text{noisy signal}} \underbrace{f(z|r)^{1_{s_i = \hat{s}}}}_{\text{observed}} \quad (14)$$

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- ▶ & use $p(X|\alpha, \beta)$ & update using Bayes' Rule:

$$p(\alpha, \beta | X) = \underbrace{p(X|\alpha, \beta)}_{likelihood} \times \underbrace{p(\alpha, \beta)}_{prior} \quad (15)$$

- ▶ to form $f(z|y, r) = \int_{\alpha \times \beta} f(z|y, r; \alpha, \beta) p(\alpha, \beta | X) d\alpha d\beta$

Calibration

- $\hat{\eta}_0$: beliefs about discrimination:

    - Black workers: discrim. affects outcomes (1985, GSS): 0.784

- μ: measure taste-based discriminatory firms:

    - Supervisors who believe Black lower ability (1977, GSS): 0.223

- Key Estimated Parameters:

    - Disc. Pen: $\gamma = 50$, Ability: σ_Q, App. Cost: σ_ν, Noise: σ_ϵ

- Targets:

    - Black-to-White rates/ratios:

        - earnings & high prestige employment ratio (CPS) - close
        - unemployment rates (CPS) - B too low, W too high
        - 25th & 75th AFQT employment rates (NLSY79) - B ↑, W ↓

    - Pooled: 95/5 earnings ratio (CPS) - close

Findings

- Set-up:

  - Explore time series of 20 cohorts.

  - Initial conditions: fix $\hat{\eta}$ and let $Z^0(q, r)$ and $\hat{P}(e|z, r; Z^0, \hat{\eta})$ converge.

- Explore the mechanisms:

  - How do observed outcomes affect worker and firm beliefs?

  - How do those beliefs affect subsequent decisions?

- Then impose Affirmative Action policy (details after mech.)

Human capital investment (1st Cohort)
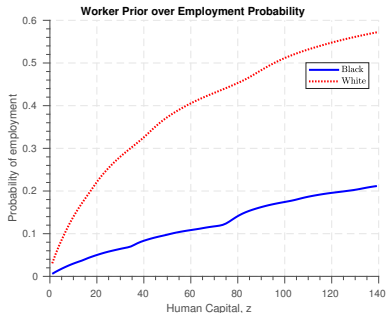
Figure: Beliefs about employment probabilities given z by race.
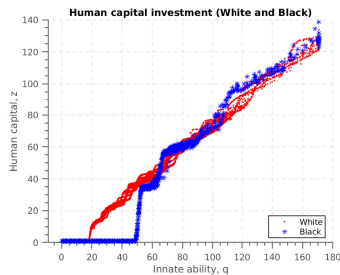
Figure: Human capital investment decisions (z) by innate ability (q) and race.

- ▶ Lower employment probability $\rightarrow$
- ▶ Less investment over key range (98th pctile).

Factors influencing hiring decisions (1st Cohort)
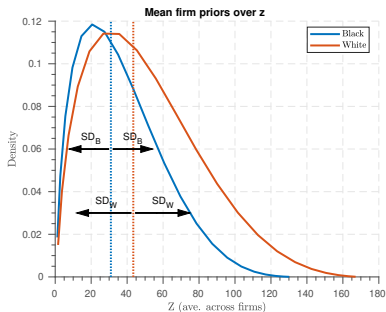
Figure: Average firm beliefs over human capital (z) by race.
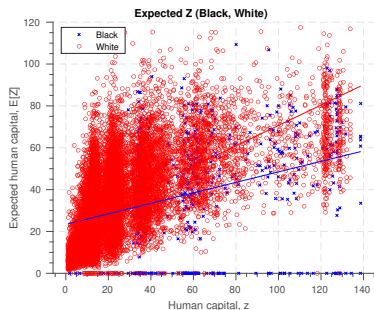
Figure: Black and White z and E[z]

▶ Firms believe avg. Black worker less qualified, no weight on high z.

▶ Bias $(E[z] - z)$ much larger for Black than White.

Discrimination beliefs and employment beliefs (1st Cohort)
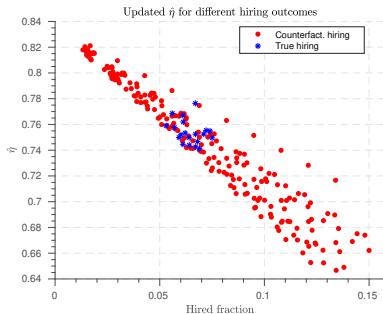
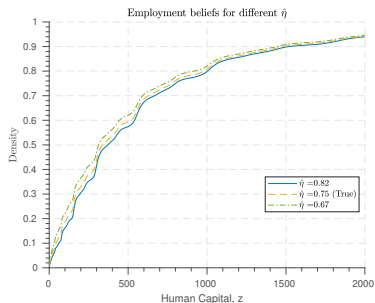Figure: Updated $\hat{\eta}$ under different hiring.

Figure: Black employment beliefs under different $\hat{\eta}$.

▶ $\hat{\eta}$ varies negatively ($\uparrow$ emp. $\downarrow \hat{\eta}$) with hiring outcomes.

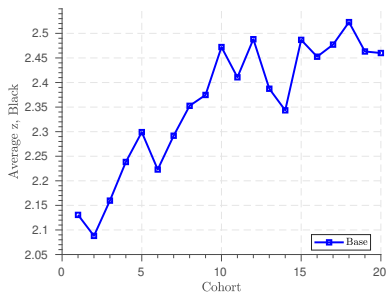▶ Lower $\hat{\eta} \rightarrow$ more optimistic $\hat{P}$.

Human Capital Investment

Figure: Human Capital z (Black)

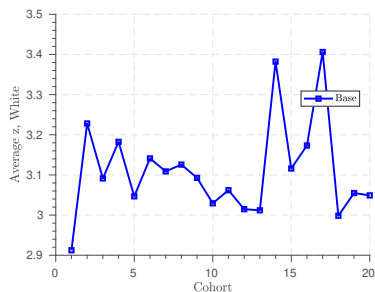Figure: Human Capital z (White)

▶ Higher levels of investment for White workers.

▶ Both vary over time, inversely related.

Policy Experiment

- ▶ Affirmative Action policy

  - ▶ *One cohort*, Black worker scores ↑ by $\zeta = \gamma$ (ad-hoc).

  - ▶ Implemented *after* investment decisions by cohort.

- ▶ Two Affirmative Action stories to explore:

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  1. Short-term direct effects:

     ▶ Do Black workers replace more qualified White workers?

     ▶ Do less qualified Black workers cause firm to revise beliefs down?

Policy Experiment

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- ▶ Two Affirmative Action stories to explore:
    1. Short-term direct effects:
        - ▶ Do Black workers replace more qualified White workers?
        - ▶ Do less qualified Black workers cause firm to revise beliefs down?

    2. Post-AA indirect effects of more initial Black hires:
        - ▶ After AA period, do additional new hires change Black beliefs?
        - ▶ Does this lead to more Black human capital investment?
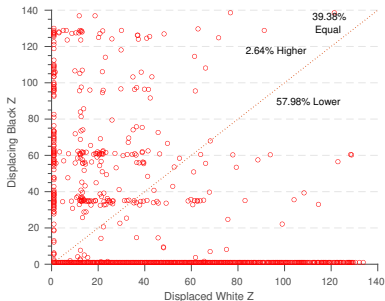   - ▶ What happens to White workers with more competition?

Initial Costs

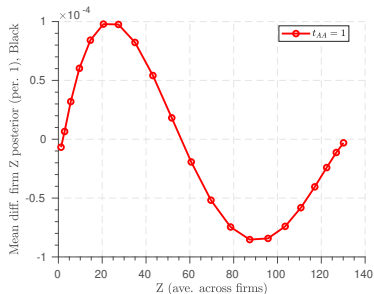Figure: White workers displaced by Black workers newly hired

Figure: Difference in firm Z beliefs (Black)

▶ 58% of White workers displaced are more qualified.

▶ Posterior firm beliefs imply firms expect lower avg. Black z.
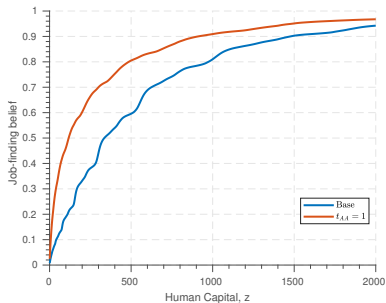
Long-Run Benefits (2nd Cohort)

Figure: $\hat{P}(e|z, B; Z^0, \hat{\eta})$ comparison.

Figure: Human capital investment decisions (z) by innate ability (q) and race.

- ▶ For next cohort, large decline in $\hat{\eta}$ (70pp, next slide)
- ▶ $\rightarrow$ upward revision in employment beliefs for all z.
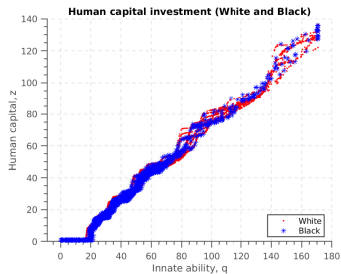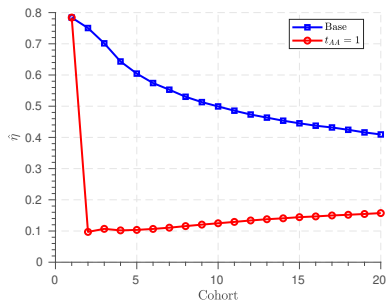- ▶ Investment mirrors White workers! (▸ baseline)

Long-Run Benefits

Figure: $\hat{\eta}$ across cohorts
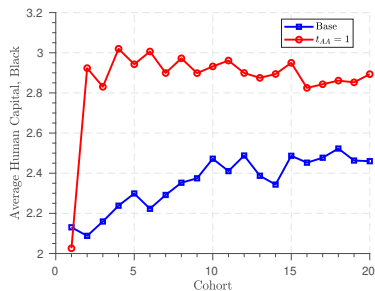

Figure: Human capital z (Black)

▶ Decrease in beliefs about discrimination persist.

▶ Large increases in Black z (averaged, including non-investment).

Overall Effects

Value	Base	$t_{AA} = 1$
Ave. $\hat{\eta}$	0.5240	0.1610
Employed Z (Post AA)	18.627	18.913
Black Z Invest	2.359	2.865
White Z Invest	3.162	3.139
Black Employed Z (Post AA)	19.565	19.646
White Employed Z (Post AA)	18.536	18.819
Black High Prestige Emp. Rate	0.0530	0.0840
White High Prestige Emp. Rate	0.0910	0.0860
Average Black Income	1.857	2.127
Average White Income	2.480	2.387

▶ Racial income inequality:

  ▶ Baseline: Black-White income ratio 75% ($\approx$ same as data).
  ▶ After Affirmative Action Policy: 89%.
  ▶ $\approx$ share accounted for by occupational choice.

▶ Emp. z: up for both Black and White!

Overview

- ► Constructed a model with

  - ► Endogenous worker beliefs about discrimination and employment;

  - ► Endogenous firm beliefs about worker productivity.

- ► Assessed the effects of Affirmative Action.

- ► Findings:

  - ► Affirmative Action may displace more qualified White workers, and negatively affect firm beliefs in short-run.

  - ► Has dynamic benefits: increases Black human capital investment by changing beliefs about employment prospects.

  - ► Overall positive effect on *both* Black and White investment.

Next Time

▶ Next time: another paper that considers beliefs in a slightly different way.

▶ Topic: How recessions affect participation.

▶ Final presentations start with 25 minutes left in class.

Discrimination and Aspirations

- ▶ Black youths who believe they face discrimination
  - ▶ aspire to less prestigious/lower pay occupations.

	Prestige Score of Career Aspiration in 1979	Aspired Occupational Income, 1970s
Black	7.0448**	4768.1849
	1.4598	2182.1669
Believes Discrimination will Affect Career=1	7.34**	13358.49***
	2.29	1681.90
Black × Believes Discrimination will Affect Career=1	-8.93***	-16090.41**
	1.35	4652.43
Test: $H_0: \beta_1 + \beta_3 = 0$	-1.881***	-11322.22**
SE	0.260	2483.498
Observations	1296	1164

Clustered standard errors in parentheses
* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$

- ▶ These careers have higher than average Black representation,
- ▶ and is realized in actual occupations at age 35. (▸ link)
- ▶ More stats about beliefs and discrimination: ▸ link   ▸ back

Discrimination and Outcomes

► Black youths who believe they face discrimination

  ► enter occupations with higher Black representation and achieve less-prestigious careers.

	Percent of Black Workers in Aspired Career	Prestige of Age-35 Occupation
Black	-0.0063	-2.4247
	0.0031	1.3379
Believes Discrimination will Affect Career=1	-0.01***	2.09
	0.00	3.45
Black × Believes Discrimination will Affect Career=1	0.03**	-4.99
	0.01	2.26
Test: $H_0: \beta_1 + \beta_3 = 0$	.024*	-7.419***
SE	0.010	1.178
Observations	1164	1293

Clustered standard errors in parentheses

* p< 0.1, ** p< 0.05, *** p< 0.01

► back

Robustness: Same Occupation as Father

▶ Same specification, with
$$1_{Aspired\ Father's\ Occ} + 1_{Black} \times 1_{Aspired\ Father's\ Occ}$$

	Prestige Score of Career Aspiration in 1979 b/se	Aspired Occupational Income, 1970s b/se
Black	7.3014**	4842.5913*
	1.3964	1956.5340
Believes Discrimination will Affect Career=1	7.22*	13148.80***
	2.34	1881.27
Black × Believes Discrimination will Affect Career=1	-8.75**	-15848.36*
	1.58	5000.00
sameAspiredOccFather=1	-2.77	-3803.78
	1.21	4461.42
Black × sameAspiredOccFather=0	0.00	0.00
	.	.
Black × sameAspiredOccFather=1	-8.87*	-3407.10
	3.22	8357.90
Observations	1296	1164
Test: 0: $\beta\_1+\beta\_3=0$	-1.453***	-11005.771**
SE	0.240	3057.215
Test: 0: $\beta\_1+\beta\_5=0$	-1.572	1435.494
SE	3.640	9697.593

Clustered standard errors in parentheses
* p< 0.1, ** p< 0.05, *** p< 0.01
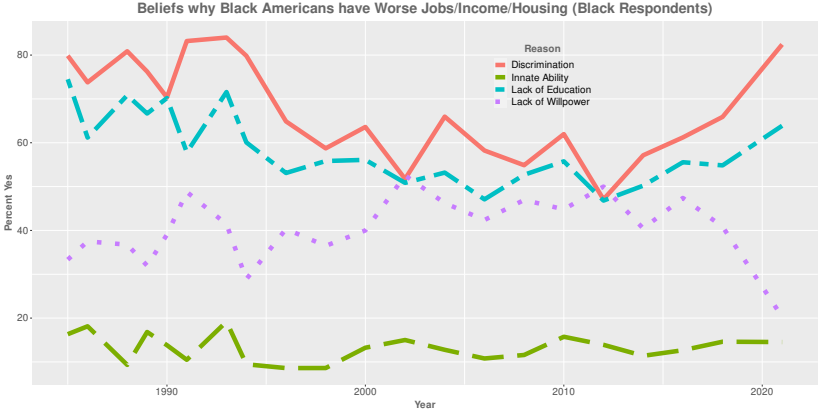
Black Beliefs about Discrimination

Figure: Black Beliefs

▶ Attribute differences to discrimination. (▶ back)
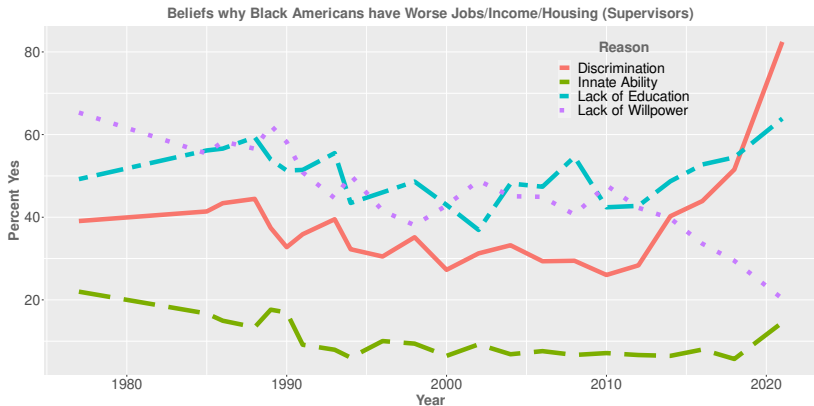
Firm Beliefs about Black Workers

Figure: Supervisor Beliefs

- ▶ (implicit assumption: Supervisors have discretion over hiring)
- ▶ Other evidence: audit studies, other responses to GSS. `▶ back`

Worker's human capital decision

▶ Endowed with race, r, innate ability, $q \sim LN(\mu_Q, \sigma_Q)$, and

▶ $\hat{\eta}$: common belief about measure of discriminators,

▶ $\hat{P}$: Prob(emp | own z, other z, discrim. beliefs) (fixed pt).

▶ Live for one period (think cohort).

▶ Investment decision:

$$V_I(z, r, \hat{P}; \hat{\eta}) = \max_z \{ E[V_A(z, r, \hat{P}; \hat{\eta})] - \frac{z^2}{2q} \} \qquad (16)$$

Worker's application decision

- Can pay pay $\nu \sim Gumbel(\sigma_\nu)$ to apply for high-prestige job;

- If not hired or don't apply, apply for "humble" job.

- High-prestige application decision:

$$V_A(z, r, \nu, \hat{P}; \hat{\eta}) = \max \left\{ \hat{P}(e|z, r; \hat{\eta})z + (1 - \hat{P}(e|z, r; \hat{\eta}))V_L + \nu, V_L \right\}$$
(17)

- $V_L = P_L z_L + (1 - P_L)b$ (think service sector)

Worker's application decision

▶ Can pay pay $\nu \sim Gumbel(\sigma_\nu)$ to apply for high-prestige job;

▶ If not hired or don't apply, apply for "humble" job.

▶ High-prestige application decision:

$$V_A(z, r, \nu, \hat{P}; \hat{\eta}) = \max\left\{ \hat{P}(e|z, r; \hat{\eta})z + (1 - \hat{P}(e|z, r; \hat{\eta}))V_L + \nu, V_L \right\} \tag{17}$$

▶ $\hat{P}(e|z, r; \hat{\eta})$ depends on beliefs about discrimination

▶ Discrim. beliefs $\hat{\eta} \uparrow \rightarrow \hat{P}(e|z, B; \hat{\eta})$ beliefs $\downarrow$

▶ $\rightarrow \hat{\eta} \uparrow \rightarrow z^* \downarrow$

Firm's hiring decision

- Hire to maximize exp. output (z), net of racial preferences

- Filter signals to find best candidate.

- Receive application, get signal of worker productivity:

$$y = ln(z) + \epsilon, \epsilon \sim N(0, \sigma_\epsilon) \qquad (18)$$

- Each applicant receives a score:

$$s(y, r, T) = E[\widetilde{z}|y, r] - 1_D^B \gamma + 1_{AA}^B \zeta. \qquad (19)$$

- 1_D^B: taste-based discriminator (reduces Black score by γ);

- 1_{AA}^B: affirmative action policy (increases Black score by ζ);

- $E[\widetilde{z}|y, r]$: Beliefs (may be biased) about the worker prod.

Firm's hiring decision

- Receive application, get signal of worker productivity:

$$y = ln(z) + \epsilon, \epsilon \sim N(0, \sigma_\epsilon) \tag{18}$$

- Each applicant receives a score:

$$s(y, r, T) = E[\widetilde{z}|y, r] - 1_D^B \gamma + 1_{AA}^B \zeta. \tag{19}$$

- $E[\widetilde{z}|y, r]$ depends on history of hires and observed signals:

$$E[\widetilde{z}|y, r] = \int zf(z|y, r)dz = \int z\frac{f(y|z, r)f(z|r)}{f(y|r)}dz \tag{20}$$

- Each firm hires $\max\{s_1, ..., s_H\}$.

- Produce worker's true z

Workers updating beliefs I

- Construct score for taste and non-taste discrim. (ϵ unknown):

$$s(y, r, T) = z + \epsilon - 1_D^B \gamma + 1_{AA}^B \zeta.$$

- Calc. $\hat{P}$ given dec. rules Z^0. Def. $F(\cdot)$ CDF of ϵ.

$\tilde{P}(e|z, r; Z^0, T) =$

$$\prod_{i=2}^{H} [\int_{\epsilon_i} \int_{q_i} \sum_{r_i=B}^{W} (\int_{\underbrace{s(Z^0(q_i, r_i) + \epsilon_i, r_i, T)}_{app.\ i\ score}}^{s_{max}} \overbrace{f(y(s, r) - ln(z))|\frac{\partial y}{\partial s(y, r)}|\, ds)}^{prob.\ 1st\ score\ higher} f(\epsilon_i) p(r_i) dQ(q_i) d\epsilon_i].$$

(21)

Workers updating beliefs I

- Construct score for taste and non-taste discrim. (ϵ unknown):

$$s(y, r, T) = z + \epsilon - 1_D^B \gamma + 1_{AA}^B \zeta.$$

- Calc. $\hat{P}$ given dec. rules Z^0. Def. $F(\cdot)$ CDF of ϵ.

$\tilde{P}(e|z, r; Z^0, T) =$

$$\prod_{i=2}^{H} [\int_{\epsilon_i} \int_{q_i} \sum_{r_i=B}^{W} (\int_{\underbrace{s(Z^0(q_i, r_i) + \epsilon_i, r_i, T)}_{app.\ i\ score}}^{s_{max}} \overbrace{f(y(s, r) - ln(z))|\frac{\partial y}{\partial s(y, r)}|\, ds)}^{prob.\ 1st\ score\ higher} f(\epsilon_i) p(r_i) dQ(q_i) d\epsilon_i].$$

$$(21)$$

$$\tilde{P}(e|B; Z^0, T) = \int_{\underline{q}}^{\bar{q}} \tilde{P}(e|z(q, B), B; Z^0, T) dQ(q)$$

- Form predicted hiring given $\hat{\eta}$ (scale by num. Black workers):

$$\tilde{P}(e|B; Z^0, \hat{\eta}) = \hat{\eta} \tilde{P}(e|B, D) + (1 - \hat{\eta}) \tilde{P}(e|B, N)$$

Calibration Results

Parameter	Value	Comment
σ_Q	1.38	SD of Innate Ability Dist.
σ_ϵ	0.816	SD of Signal Noise
σ_ν	1.38	SD of Application Taste Shock
γ	50	Taste-Based Discrimination Score Penalty
$Pr(e_L)$	0.788	Low Prestige Employment Probability
μ	0.221	Supervisor Responses about Lower Black Ability (GSS, 1977)
$\hat{\eta}_0$	0.784	Black Responses about Labor Market Discrimination (GSS, 1985)
b	0.4	Approx UI Replacement Rate (US)
z_L	1.00	Normalization
ζ	50	Assumption
μ_Q	1.00	Normalization

Calibration Fit

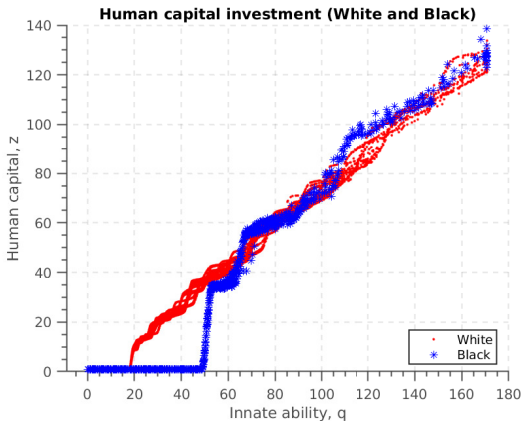| Moment	Data	Model
Black-to-White Earnings Ratio	0.6273	0.6591
95/5 Earnings Ratio (Pooled)	5.8203	5.8454
Black Unemployment Rate	0.0597	0.0401
White Unemployment Rate	0.0285	0.0390
Black Employment Rate (25th AFQT Pctile)	0.9100	0.9533
Black Employment Rate (75th AFQT Pctile)	0.9600	0.9591
White Employment Rate (25th AFQT Pctile)	0.9600	0.9622
White Employment Rate (75th AFQT Pctile)	0.9900	0.9595
Ratio of Black-to-White High Prestige Employment Rates	0.5623	0.5149

Human capital investment Baseline

Figure: Human capital investment decisions (z) by innate ability (q) and race.